

Abstract

Topology & Topological Space

Let X be a nonempty set and τ be a family of subsets of X (i.e., $\mathcal{P}(X)$).

We say τ is topology on X if satisfy the following conditions:

$$(1) X, \emptyset \in \tau$$

$$(2) \text{If } U, V \in \tau, \text{ then } U \cap V \in \tau$$

The finite intersection of elements form τ is again an element of τ .

$$(3) \text{If } U_a \in \tau; a \in A, \text{ then } \bigcup_{a \in A} U_a \in \tau \quad \forall a \in A$$

The arbitrary (finite or infinite) union of elements of τ is again element of τ .

We called a pair (X, τ) **topological space**.